RFKNN: ROUGH-FUZZY KNN FOR BIG DATA CLASSIFICATION

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Abstract: The K-nearest neighbors (kNN) is a lazy-learning method for classification and regression that has been successfully applied to several application domains. It is simple and directly applicable to multi-class problems however it suffers a high complexity in terms of both memory and computations. Several research studies try to scale the kNN method to very large datasets using crisp partitioning. In this paper, we propose to integrate the principles of rough sets and fuzzy sets while conducting a clustering algorithm to separate the whole dataset into several parts, each of which is then conducted kNN classification. The concept of crisp lower bound and fuzzy boundary of a cluster which is applied to the proposed algorithm allows accurate selection of the set of data points to be involved in classifying an unseen data point. The data points to be used are a mix of core and border data points of the clusters created in the training phase. The experimental results on standard datasets show that the proposed kNN classification is more effective than related recent work with a slight increase in classification time.

Keywords: classification, kNN, big data, clustering, fuzzy sets, rough sets.

1. INTRODUCTION

The K-Nearest Neighbors (kNN) is a renowned data mining technique. It is applied to both classification and regression tasks in several application domains [1], [2]. Traditional kNN classification algorithm works as follows: A data point is classified by identifying the k neighbors of this data point and counting the number of neighbors from each class. The data point is assigned to the class to which the majority of the k neighbors belong. k is a positive integer, typically small and depends on the size and distribution of the input data. When \( k = 1 \), then the unseen data point is assigned to the class of its nearest neighbor. In binary (two classes) classification problems, it is meaningful to choose \( k \) to be an odd number to avoid tied votes. One of the key advantages of nearest neighbor approach is that the density function for each target data point is estimated locally and differently instead of being estimated once for the entire instance space [3]. From its definition, it is clear that it is simple (easy to implement), multi-class (can deal with datasets having more than two classes), memory-based (training set stored in memory without explicit generalization), and non-parametric method (no assumptions about the input data).

In [4], the performance of different similarity measures that can be used in the KNN algorithm, are evaluated. In [5], a new affinity function for distance measure between a test point and a training point based on local learning is introduced. A Bayesian method is investigated in [6] for estimating a proper value for \( k \) in kNN algorithm.

In [7], an adaptive parameter-free neighborhood construction algorithm based on density and connectivity is proposed to tackle the problem of estimating the set of neighbors for each data point without a priori information about the dataset. A recent approach in [8] proposed an algorithm termed CM-kNN that learns a correlation matrix to reconstruct test data points by training data to assign different \( k \) values to different test data points and applied the proposed algorithm to regression and missing data imputation.

When traditional KNN decision rule is applied to unbalanced data, there is a tendency to assign an unseen object to the majority class label. Several strategies for selecting the objects to be dimmed from the majority class are proposed in [9]. Another approach is resizing the input dataset by either under sampling majority class, oversampling the minority class or by doing both at the same time (hybrid) [10], until the data is balanced.

Also, kNN is used in future selection as in [11] where a neighborhood rough set technique is used to rank and prioritize lists of potential tumor-related genes from the genetic profile. Other research studies that use an ensemble of KNN classifiers as a gene selector are found in [12] and [13].

Although the kNN algorithm has shown outstanding performance in a wide variety of problems, it lacks the scalability to manage (very) large datasets. The kNN suffers high computational complexity. The complexity to find the nearest neighbor training example of a single test instance is \( O(nd) \), where \( n \) is the number of training objects and \( d \) is the number of attributes (features). Also, an extra complexity \( O(k \log k + n) \) to select the \( k \) closest neighbors. Furthermore, the kNN model requires the training data to be stored in memory for a rapid computation of the distances.

An example for early work for accelerating kNN is found in [1] where the fat \( k \) closest vectors are identified in the design set of a kNN classifier for each input vector by performing a partial distance search in the wavelet domain.

However, early work does not suit very large datasets. This motivates researchers in the big data area to distribute the processing of a kNN classifier over a cluster of nodes to be suitable for the application of big data [14].

This paper focuses on scaling the kNN classification to suit the application of big data. Existing approaches for scaling kNN can be categorized into two main approaches: fast finding the nearest samples [15] and selecting representatives samples (or removing some samples) to reduce the calculation of kNN [16]. The most related technique for the proposed technique is a recent approach for scaling kNN based on partitioning [17]. Landmark-
based Spectral Clustering (LSC) is used in [17] for partitioning the input data. Landmarks for LSC are selected either randomly or using k-means and the corresponding techniques are termed as RC-kNN and LC-kNN respectively.

In this paper, we propose to integrate the principles of rough sets [18] and fuzzy sets [19] into the approach in [17]. This allows distinguishing between core and border objects in each produced cluster. In the classification of an unseen object, a proper set of data points are efficiently and effectively selected as a union of one core partition and several border partitions that are necessary for classifying the unseen data point depending on its membership in the clusters which are produced in the training phase. Two techniques are proposed termed as RC-RFkNN and LC-RFkNN for randomly or using k-means landmarks for LSC clustering respectively. Experimental results show that RC-RFkNN and LC-RFkNN achieve an enhancement in terms of classification accuracy over RC-kNN and LC-kNN respectively.

The remainder of this paper is organized as follows. Section II details the proposed method along with the necessary background. Then, Section III presents the experimental setup and results with analysis of results. Finally, Section IV outlines the conclusions drawn in this work.

II. MATERIALS AND METHODS

A. Rough Set and Fuzzy Set

Let a target set \( X \) to be represented using attribute subset \( P(X); \overline{P}(X) \) are two crisp sets representing the lower boundary of \( X \), and the upper boundary of the target set \( X \) respectively. The tuple \( <P(X), \overline{P}(X)> \) composed of the lower and upper approximation of a set \( X \subseteq U \) is called a rough set [18]. In the remaining of this paper, we refer to the lower and upper approximation of a cluster \( C_i \) as \( L(C_i) \) and \( U(C_i) \) respectively. The lower approximation of a cluster \( L(C_i) \) is an unadventurous approximation consisting of only those objects which can definitely be identified as members of this cluster. The upper approximation includes all data points that might be members of the target set. (Some data points in the upper approximation may not be members of the target set).

The lower approximation contains objects that are members of the target set with probability equals 1, while the upper approximation contains objects that are members of the target set with non-zero probability. As shown in Fig. 1, the boundary region, given by set difference \( U(C_i) - L(C_i) \) consists of those objects that can neither be ruled in nor ruled out as members of the target cluster. A fuzzy set \( F \) [19] of \( U \) is a mapping from \( U \) into the unit interval \([0, 1]\):

\[
\mu_F : U \rightarrow [0, 1],
\]

The crisp set that contains all the elements of \( U \) that have a nonzero membership value in \( F \) is called as the support of the fuzzy set \( F \).

A function mapping of all the elements in a crisp set into real numbers in \([0, 1]\) is called a membership function. The larger value of the membership function represents the higher degree of the membership. It means how closely an element resembles an ideal element. Membership functions can represent the uncertainty using some particular functions. In the following sections Border(Ci) refers to \( U(C_i) - L(C_i) \) while Core(Ci) refers to \( L(C_i) \).

B. Soft Clustering

The algorithm k-means [20] which is used in [17] as the final step for partitioning the input big dataset always results in memberships \([0,1]\). In the proposed algorithm we need fuzzy memberships i.e. positive grades of membership \( \mu_y \) for each object \( x_j \) in cluster \( i \). If we use fuzzy clustering algorithm such as fuzzy k-means [21], an object may belong to all clusters with varying degree of belongingness. The pitfall is that all memberships are used in computing new centers which in turn used in computing new memberships at each iteration of the algorithm and hence small memberships still have an effect on the whole process. Furthermore, in the proposed algorithm we are interested in objects that have enough high membership to be considered core or border objects.

In [22] three mathematical models for soft clustering (semi-fuzzy) along with three algorithms for implementing them are introduced. The first model limits the fuzziness to a smaller subset of the available clusters. The second and third models allow a pattern to be associated with the proper number of clusters based on a proper choice of threshold value on distance or membership respectively. The concept of semi-fuzzy clustering is applied to several problems in bioinformatics [23], [24], [25]. In this paper the third model of soft (semi-fuzzy) clustering introduced in [22] will be applied instead of the k-means in [17].

C. RC-kNN and LC-kNN algorithms [17]

The most related technique for the proposed technique is a recent approach for scaling KNN in [17] which is based on Landmark-based Spectral Clustering (LSC). LSC starts by computing \( p \) landmarks by using the resulting centers of running the k-means algorithm several times (or by using random sampling). Then, constructs an affinity matrix \( W \) between data points and landmark samples. The \( v \) representative samples are computed using the eigenvectors of a matrix derived from \( W \). The overall time complexity for LSC is \( O(p^3 + p^3n) \). For each test sample, its nearest cluster center is identified and its corresponding cluster is used as the new training dataset for this sample.

D. Proposed Algorithm

Table 1 describes the pre-classification steps of the proposed algorithm. Steps 1-4 in Table 1 represent the steps of LSC algorithm which are the same as in [17]. After computing \( p \) landmarks in step 1, \( r \) nearest landmarks for each object \( x_i \) are identified, denoted \( Z_{x_i} \). A matrix \( W \) of size \( n \times r \) is computed as follows:
Let \( W = D^{0.5} W \) where \( D \) is the row sum of \( W \). Note that each column of \( W \) sums up to 1 and thus the degree matrix of \( W W^T \) is 1.

The matrix \( V \) in step 4 is called as right singular vectors of \( W W^T \). \( V \) can be computed as follows:

\[
V = U^{-1} W^T
\]  

(2)

Where \( U = [u_1, u_2, \ldots, u_m] \) is called as the left singular vectors of the first k eigenvectors of \( W W^T \).

In step 5, soft k-means is applied instead of k-means.

### III. Experimental Results

#### A. Input Data

As mentioned in the previous sections, our proposed algorithm is an extension of RC-kNN and LC-kNN. Thus, in order to show the effectiveness of LC-RFkNN and RC-RFkNN algorithms, we took the kNN as the baseline and made a comparison between kNN, LC-kNN, RC-kNN, LC-RFkNN and RC-RFkNN using three large multi-class datasets listed in table 3 from UCI [26] and LIBSVM [27].

#### B. Performance Measure

In the following experiments, the empirical accuracy is used for estimating the quality of the proposed classifier. Let \( g \) be a classifier, and \( x_i \) and \( y_i \) be respectively a test sample and its class label. Let \( g(x_i) \) be the predicted class for \( x_i \) using the classifier \( g \). The accuracy can be calculated as follows:

\[
\text{Accuracy} = \frac{1}{m} \sum_{i=1}^{m} g(x_i) = y_i \quad (4)
\]

The accuracy in Eq. (1) is calculated as total number of correct prediction divided by the total number of data points to be classified. Computing the accuracy on imbalanced data using Eq. (1) is a misleading performance measure.

\[
\text{Accuracy} = \frac{1}{m} \sum_{i=1}^{m} w_y g(x_i) = y_i \quad (5)
\]

where \( w_y \) be the weight of the class \( y \) as follows:

\[
w_y = \frac{1}{n} \sum_{i=1}^{n} w_{xy} \quad (6)
\]

By computing TP, FP, and FN, for each class \( i \) other.
performance measures can be easily computed as macro and micro average over all classes. TP<sub>i</sub> refers to the number of instances of class <i>i</i> that are correctly classified as class <i>i</i>. FP<sub>j</sub> is the number of instances of class <i>j</i> (i ≠ j) that are incorrectly classified as class <i>i</i>. FN<sub>j</sub> is the number of instances of class <i>i</i> that are incorrectly classified as class <i>j</i> (i ≠ j). In order to be able to compare with RC-kNN and LC-kNN, the accuracy is used in evaluating RFkNN as it was the only measure used in [17].

C. Experimental results for different value of <i>m</i>

As mentioned before the proposed algorithms RC-RFkNN and LC-RFkNN are based on partitioning the datasets into several clusters. Each cluster in the proposed algorithm is seen as two crisp partitions core and border. The no. of clusters <i>m</i> is very important to the proposed algorithm as it was very important to RC-kNN and LC-kNN algorithms [17].

The value of <i>m</i> directly affects the classification time and accuracy. Thus, in order to select a proper value of <i>m</i>, a group of experiments were conducted on the three standard datasets listed in table 3. By choosing different values of <i>m</i> for LC-RFkNN and RC-RFkNN. Specifically, the LC-RFkNN and RC-RFkNN in this group of experiments were carried out on the three datasets with <i>m</i>=10, 15, 20, 25 and 30, respectively as shown in Fig. 2-4. The values plotted for RC-kNN and LC-kNN are those reported in [17].

From Fig. 2–4, we found that the two proposed algorithms LC-RFkNN and RC-RFkNN outperform the corresponding algorithms LC-kNN and RC-kNN respectively in terms of accuracy. The accuracy of the algorithm kNN is the upper bound for the other four algorithms as expected. The gain in performance for RC-RFkNN over RC-kNN was much higher than the gain in performance with LC-RFkNN over LC-kNN.

RC-RFkNN is higher by 3.6%, 1% and 2.4% than RC-kNN for <i>m</i>=15 on LETTER, PENDIGITS and UPS respectively. It is clear from the figures 2-4 that identifying core and border objects helps increasing the performance in terms of accuracy. The runtime of the proposed algorithm cannot be directly compared to those reported by [17]. However, the runtime of the proposed classification algorithm is not expected to be much higher than LC-kNN or RC-kNN as both algorithms needs to compute the distance to the centers of the <i>m</i> partitions. The proposed algorithm has an advantage of having stable performance for large values of <i>m</i> as shown above figures. Large value of <i>m</i> means less classification time since the average partition size is smaller.

D. Tuning the parameter <i>k</i>

This section reports the results of a group of experiments which were conducted on LETTER dataset in order to select a proper value for the number of nearest neighbors <i>k</i>. <i>k</i> is varied between 1 to 9 by step equals 2. Each point in the figures 5–6 represents the mean of 15 results with the same parameters. From Fig. 5 and 6, the classification accuracy slightly increases from <i>k</i>=1 to <i>k</i>=3 after that with the increase of the value of <i>k</i>, the overall of classification accuracy decreases. Furthermore, the higher the no. partitions <i>m</i>, the higher the decrease in the classification accuracy with higher value of <i>k</i>. Hence, the difference between the samples is significant and the classification accuracy will reduces. We can make a conclusion that <i>k</i>= 1 or 3 is suitable choices for <i>k</i> in his case. In general, the value
of k may be set as small as possible since high value of k means increase in runtime also. The value of k is extremely training-data dependent, changing the position of a few training data may lead to a significant loss of performance. Including the border objects of other partitions in addition to the the nearest partition increases the classification accuracy of the proposed method. Besides, it reduces the sensitivity of RC-RFkNN and LC-RFkNN for larger value of m.

The performance of the proposed methods for both k = 1 and k = 3 were high while for RC-kNN and LC-kNN the performance degrades for value of k higher than 1.

The performance for high value of m compared to RC-kNN and LC-kNN. As the number of partitions increases, the average size of NewX decreases resulting in a decrease in classification time with acceptable performance as shown in Fig. 2-6. Therefore, according to the experimental results, we may conclude that both RC-RFkNN and LC-RFkNN work well in terms of classification accuracy and time.

### Table 4 Classification Accuracy of RFkNN compared to three algorithms on three datasets for m=10 and k=1

<table>
<thead>
<tr>
<th>Dataset</th>
<th>RC-kNN</th>
<th>LC-kNN</th>
<th>kNN</th>
<th>RFkNN</th>
<th>RC-RFkNN</th>
</tr>
</thead>
<tbody>
<tr>
<td>LETTER</td>
<td>78.92</td>
<td>94.95</td>
<td>95.18</td>
<td>81.53</td>
<td>95.08</td>
</tr>
<tr>
<td>PENDIGIT</td>
<td>94.52</td>
<td>97.21</td>
<td>97.80</td>
<td>94.61</td>
<td>97.38</td>
</tr>
<tr>
<td>UPS</td>
<td>90.27</td>
<td>93.55</td>
<td>94.82</td>
<td>92.31</td>
<td>93.55</td>
</tr>
</tbody>
</table>

### IV. CONCLUSION AND FEATURE WORK

Several existing efficient kNN classification algorithms are based on partitioning such as in [17]. This paper proposes an enhancement over these techniques by using the rough fuzzy set while conducting the clustering algorithm to separate the whole dataset into several parts. After clustering, each produced cluster is divided into two partitions: border and core. Only one core partition along with one or more border partitions are used in classifying unseen objects. The number of border partitions to be used depends on the unseen object's memberships in the clusters that are produced in the training phase. The proposed algorithm is a generalization of existing RC-kNN and LC-kNN algorithms [17]. Experimental studies are carried to select a suitable value for the input parameters for each dataset such as the number of clusters to be produced in the training phase m and the number of neighbors to be used in the classification phase k. The traditional kNN is used as the baseline and several experiments are conducted on three standard datasets to compare the proposed RC-RFkNN and LC-RFkNN to the most related algorithms kNN, LC-kNN and RC-kNN. The experimental results showed that the proposed LC-RFkNN and RC-RFkNN outperform the corresponding techniques LC-kNN and RC-kNN respectively. The gain in performance in terms of accuracy with RC-RFkNN over RC-kNN was higher than LR-FkNN over LC-kNN. The proposed approach inherits its efficiency from RC-kNN and LC-kNN since the added steps to both the training and testing phase are very simple. As a feature work, a new solution to perform an approximate k-nearest neighbors classification based on Spark may be developed to deal with big data [28]. We will also investigate the influence of using rough fuzzy set on the balance of accuracy and computation efficiency.

V. REFERENCES


